

# **Physics Potential of Muon Factory and Neutrino Factory Based on FFAGs**

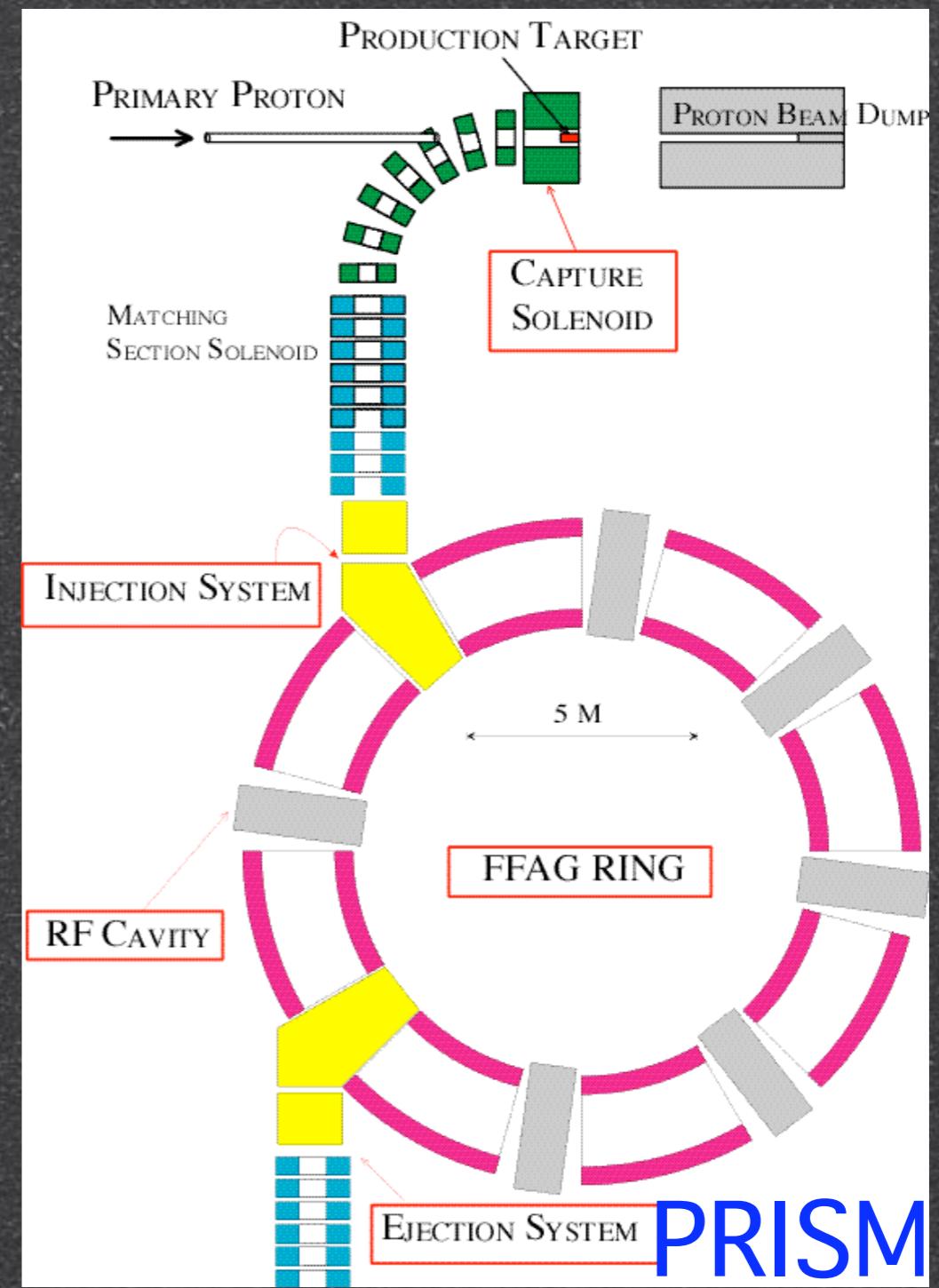
Yoshitaka KUNO  
Osaka University

TRIUMF FFAG Symposium,  
April 14th 2004, at TRIUMF

# What are Muon and Neutrino Factories ?

## Muon Factory

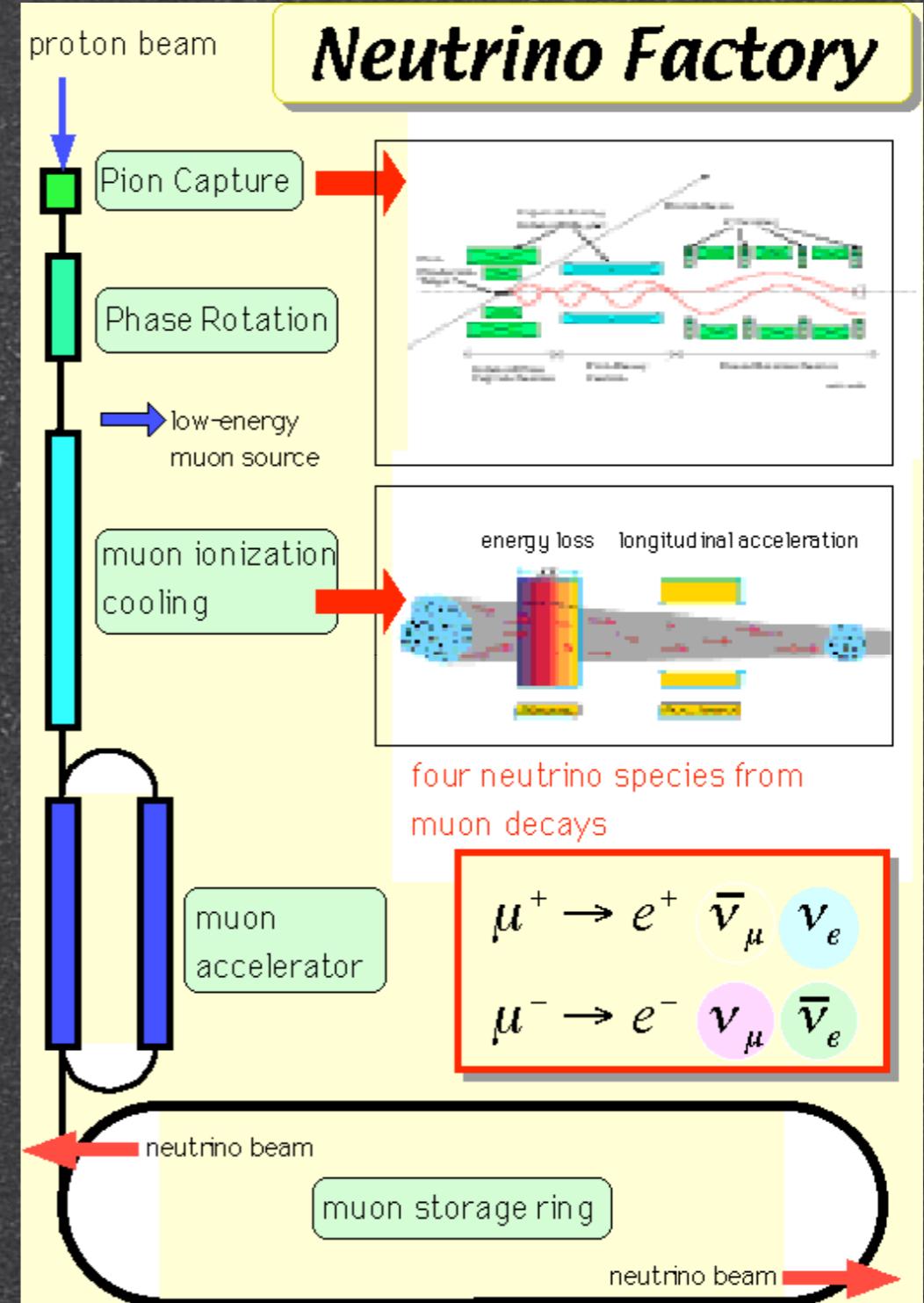
- high intensity
  - $10^{12} - 10^{14} \mu^\pm/\text{sec}$
- a MW proton machine needed
- high brightness
- narrow E width
- beam treatment (FFAG)
- high purity (no pions)
- dedicated to types of experiments?



# What are Muon and Neutrino Factories ?

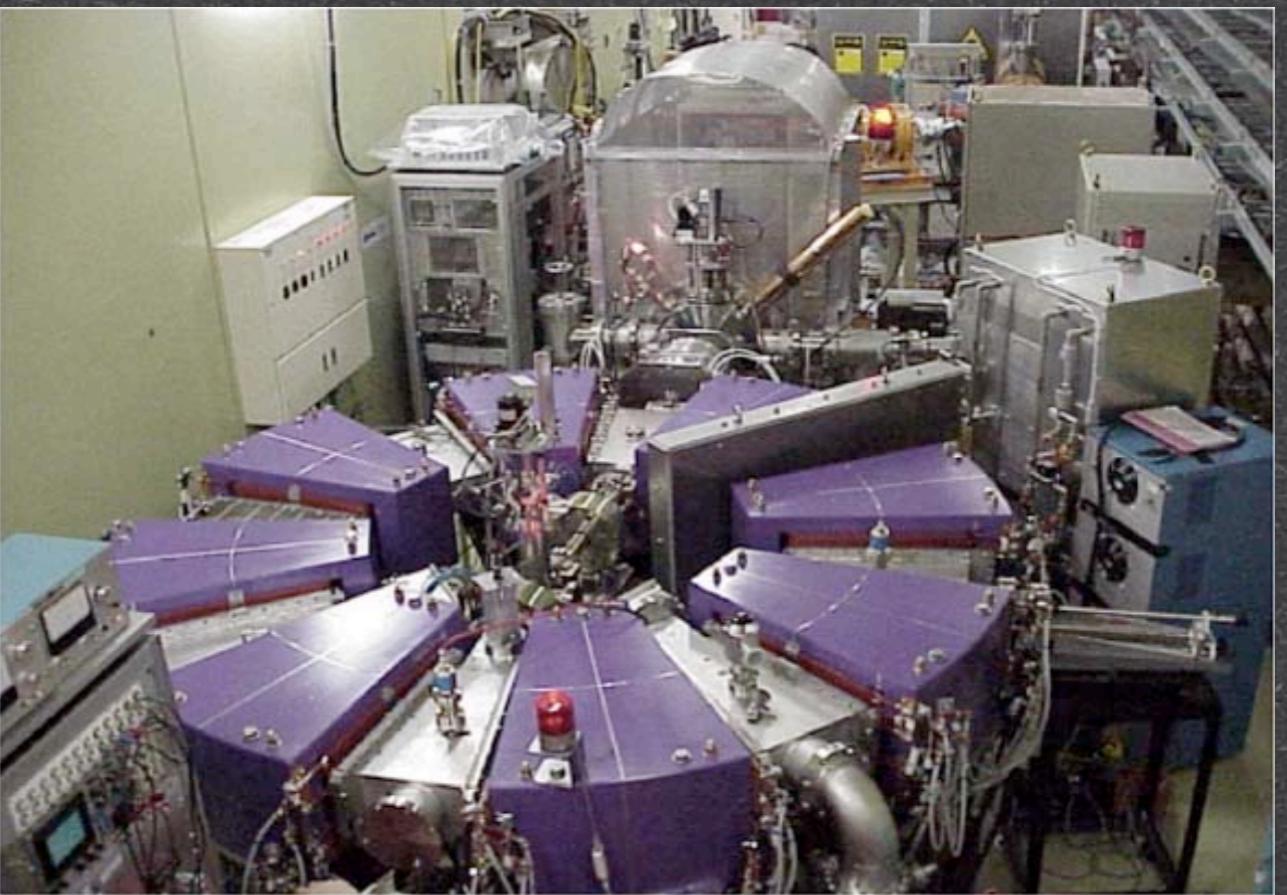
## Neutrino Factory

- high intensity
- $10^{19} - 10^{21} \nu/\text{year}$
- a MW proton machine needed
- use decays of muons accelerated to high energy (**FFAG**) and stored in the ring
- all four types available
- high energy neutrinos
- known beam quality



# FFAG Advantages

- Large Acceptance
  - Both Longitudinal and Transverse directions
  - strong focusing
- Fast Acceleration
  - due to fixed magnetic field



fast proton FFAG @KEK (2001)

Suitable to Muon Acceleration

# Outline

- Introduction to Flavor Particle Physics
- Muon Factory (only specific topics)
  - Muon Lepton Flavor Violation (PRISM)
  - Muon Electric Dipole Moment (PRISM-II)
  - J-PARC Case
- Neutrino Factory
  - Physics Motivation
- PRISM R&D Status
- Conclusion / Announcement

# *Flavor Particle Physics*

# Look up from Low to High

energy scale (GeV)

$10^{20}$   
 $10^{18}$   
 $10^{16}$   
 $10^{14}$   
 $10^{12}$   
 $10^{10}$   
 $10^8$   
 $10^6$   
 $10^4$   
 $10^2$   
 $10^0$

GUT

RH Neutrinos

Standard Model

SUSY

Super String

Supergravity

SUSY GUT

Minimum SUSY  
Standard Model  
(MSSM)

Flavor Structure of Quarks and Leptons

# Flavor Physics

supersymmetry

Muon Lepton  
Flavor violation

quarks

squarks

$$\begin{pmatrix} V_{cd} & V_{us} & V_{ub} \\ V_{cb} & V_{ts} & V_{tb} \end{pmatrix}$$

$$\begin{pmatrix} \Delta\tilde{m}_e^2 & \Delta\tilde{m}_{12}^2 & \Delta\tilde{m}_{13}^2 \\ \Delta\tilde{m}_{21}^2 & \Delta\tilde{m}_\mu^2 & \Delta\tilde{m}_{23}^2 \\ \Delta\tilde{m}_{31}^2 & \Delta\tilde{m}_{32}^2 & \Delta\tilde{m}_\tau^2 \end{pmatrix}$$

A Muon Factory and a Neutrino Factory  
are very important

neut

$$\begin{pmatrix} Y_1 e^{i\Phi_1} & & \\ & Y_2 e^{i\Phi_2} & \\ & & Y_3 e^{i\Phi_3} \end{pmatrix}$$

$$\begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \begin{pmatrix} 1 \\ e^{i\phi_1} \\ e^{i\phi_2} \end{pmatrix}$$

$$\begin{pmatrix} \Delta\tilde{m}_e^2 & \Delta\tilde{m}_{12}^2 & \Delta\tilde{m}_{13}^2 \\ \Delta\tilde{m}_{21}^2 & \Delta\tilde{m}_\mu^2 & \Delta\tilde{m}_{23}^2 \\ \Delta\tilde{m}_{31}^2 & \Delta\tilde{m}_{32}^2 & \Delta\tilde{m}_\tau^2 \end{pmatrix}$$

Leptogenesis

Standard Model

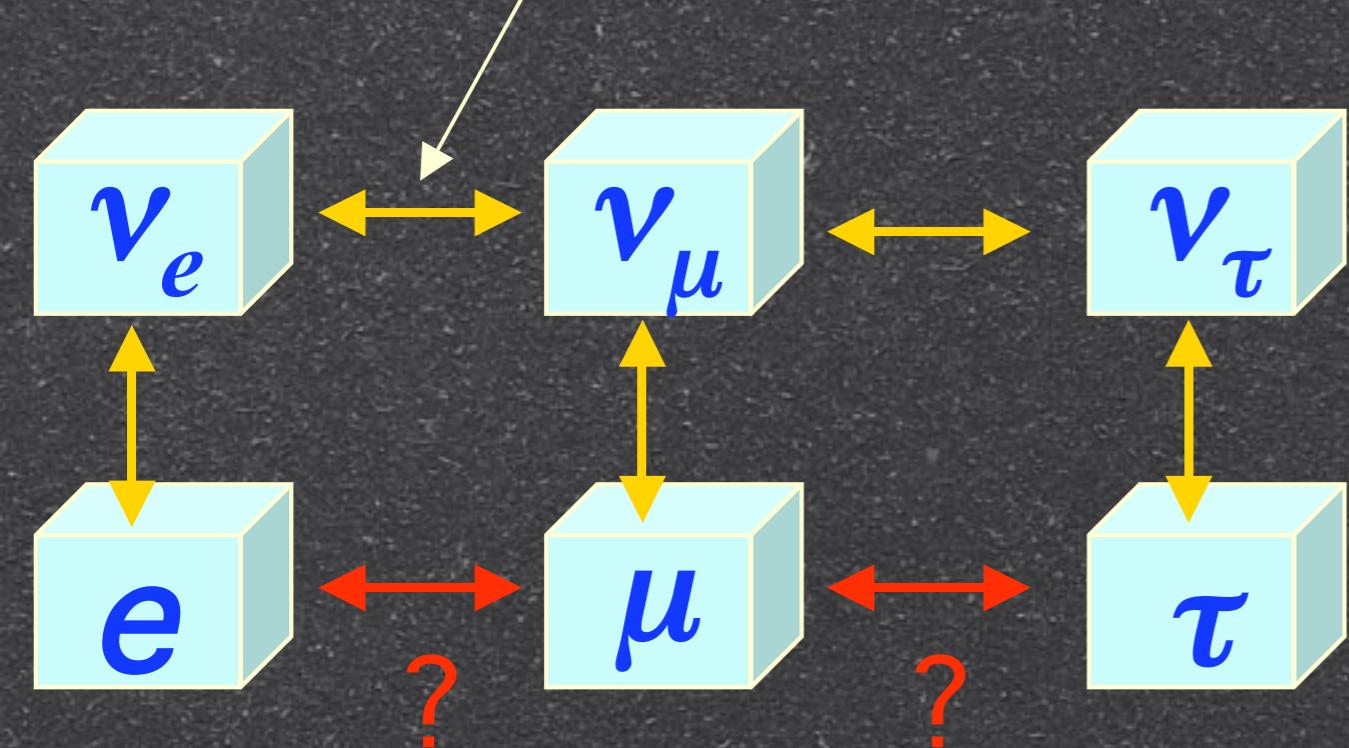
New physics

# *Muon Lepton Flavor Violation*

# Charged Lepton Flavor Violation (cLFV)

Flavor changing processes  
in charged lepton ?

Neutrino oscillation



- Example:  $\mu^+ \rightarrow e^+ \gamma$

muon flavor	-1	0
electron flavor	0	-1

Not be observed yet !

- Example:  $\mu^+ \rightarrow e^+ e^- e^+$

muon flavor	-1	0	0	0
electron flavor	0	-1	+1	-1

Not be observed yet !

# Contribution to LFV from Neutrino Oscillation

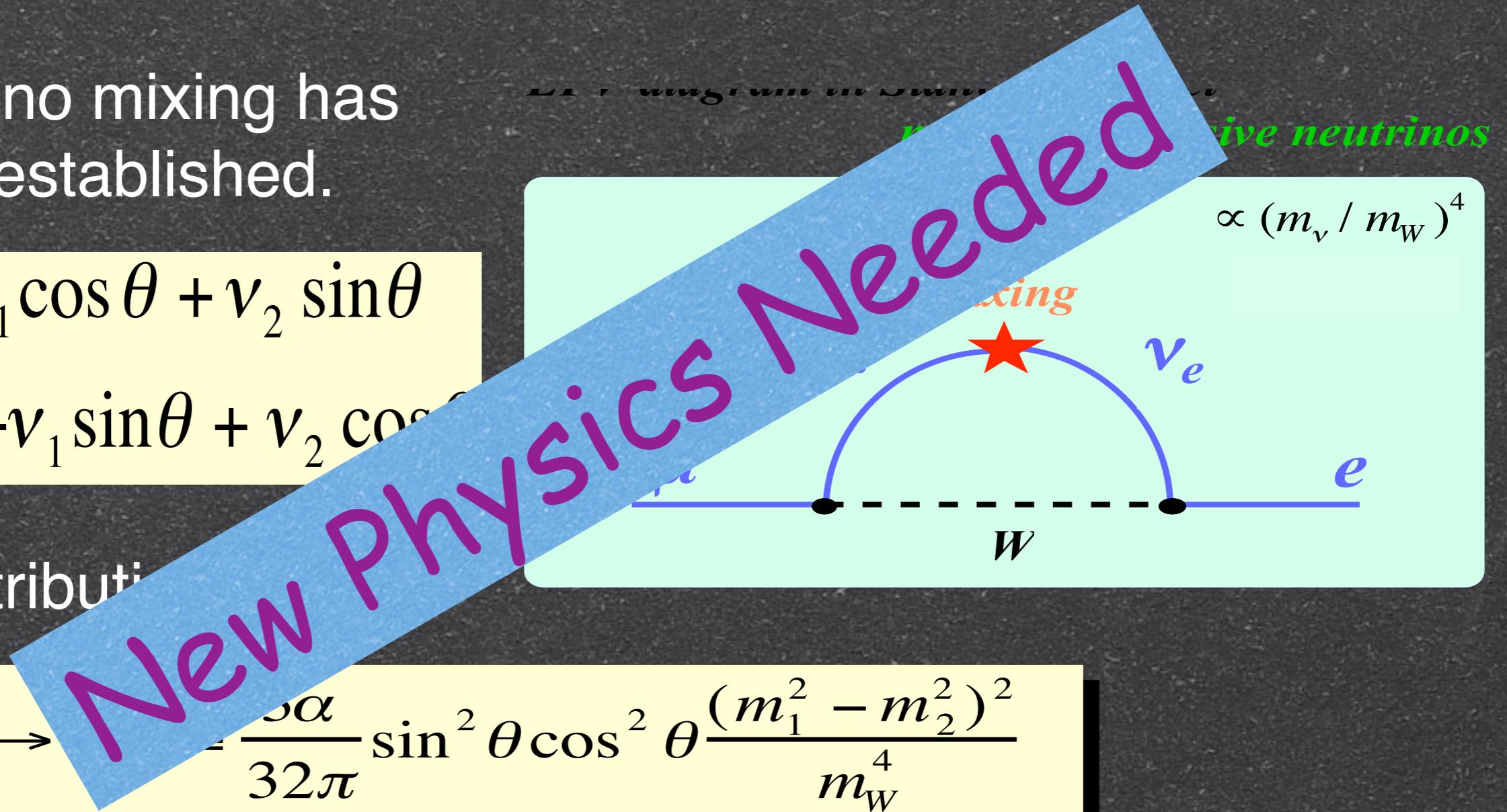
Neutrino mixing has been established.

$$\nu_e = \nu_1 \cos \theta + \nu_2 \sin \theta$$

$$\nu_\mu = -\nu_1 \sin \theta + \nu_2 \cos \theta$$

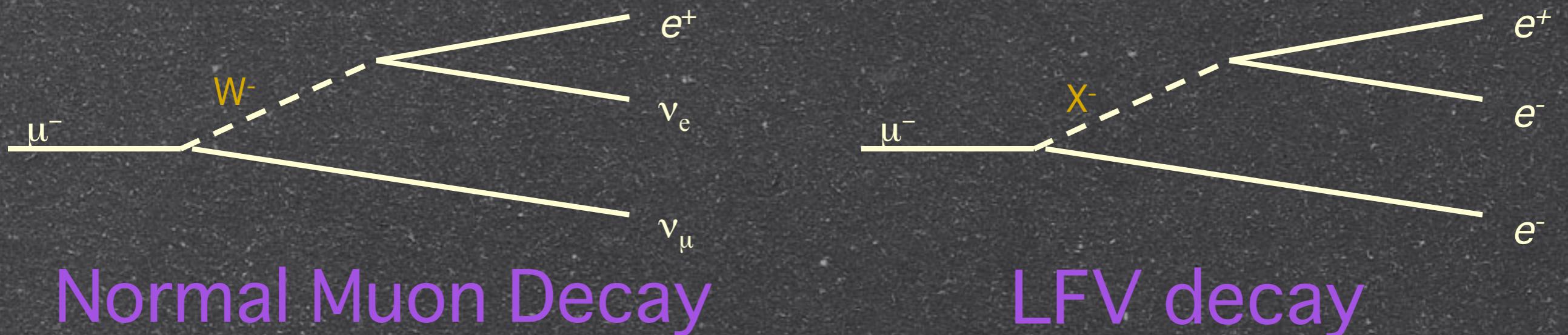
Contributions

$$B(\mu \rightarrow e) = \frac{5\alpha}{32\pi} \sin^2 \theta \cos^2 \theta \frac{(m_1^2 - m_2^2)^2}{m_W^4}$$



Very Small ( $10^{-50}$ )

# High Energy Scale by Rare Decays



Normal Muon Decay

LFV decay

$$\frac{\Gamma(\mu \rightarrow eee)}{\Gamma(\mu \rightarrow e\nu\nu)} = \frac{G_X^2}{G_F^2} = \left( \frac{m_W}{m_X} \right)^4 \leq 10^{-12}$$

$$m_X \geq 10^3 m_W \approx 100 TeV (= 10^{15} eV)$$

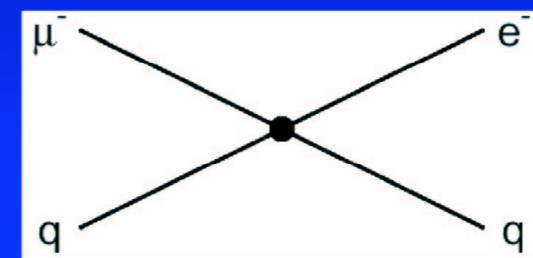
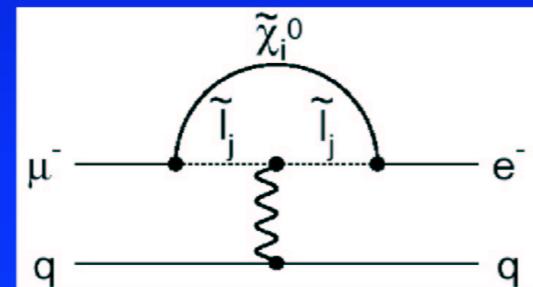
Rare decay searches at low energy could access physics at high energy scale which cannot be reached by accelerators.

# LFV Models beyond SM

## Sensitivity to Different Muon Conversion Mechanisms

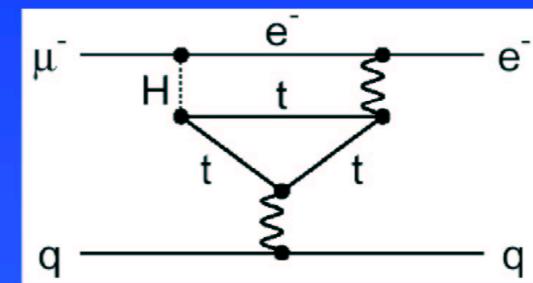
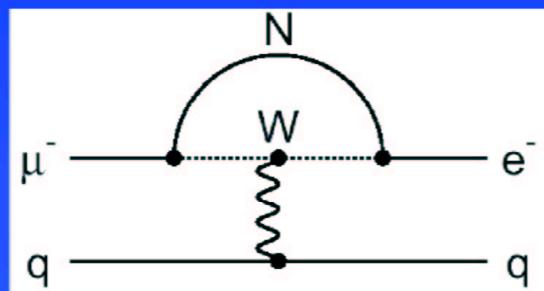


Supersymmetry  
Predictions at  $10^{-15}$



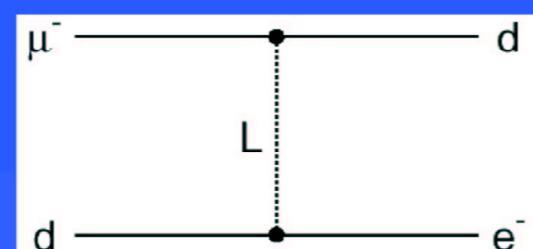
Compositeness  
 $\Lambda_c = 3000 \text{ TeV}$

Heavy Neutrinos  
 $|U_{\mu N}^* U_{e N}|^2 =$   
 $8 \times 10^{-13}$

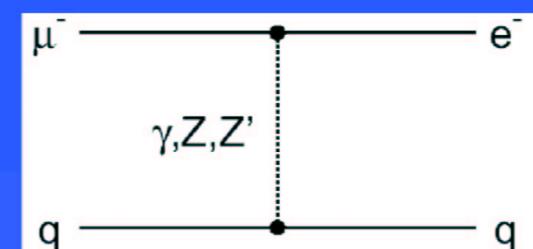


Second Higgs  
doublet  
 $g_{H\mu e} = 10^{-4} \times g_{H\mu\mu}$

Leptoquarks  
 $M_L =$   
 $3000 (\lambda_{\mu d} \lambda_{ed})^{1/2} \text{ TeV}/c^2$



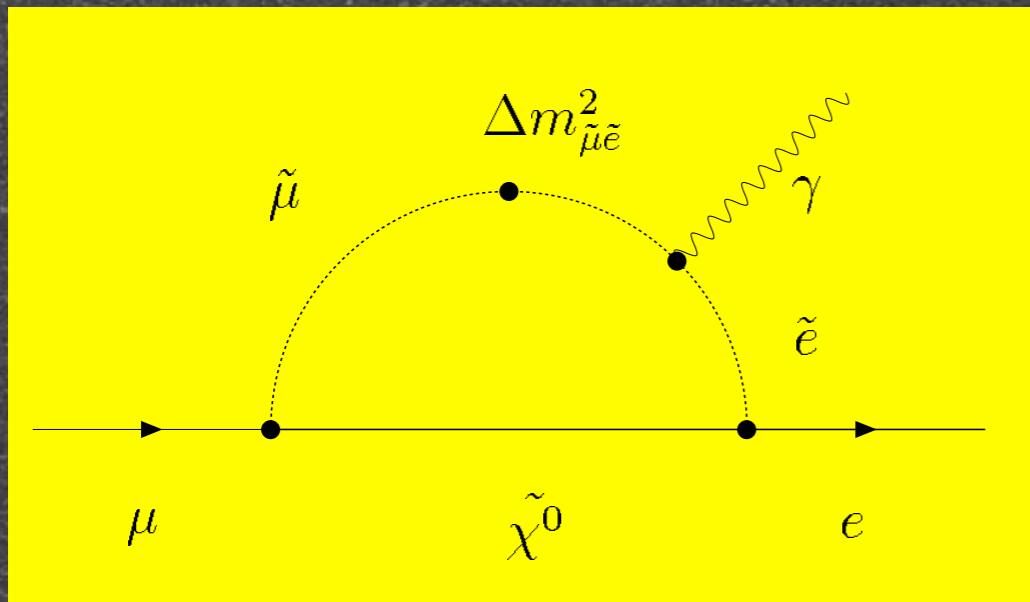
After W. Marciano



Heavy  $Z'$ ,  
Anomalous  $Z$   
coupling  
 $M_{Z'} = 3000 \text{ TeV}/c^2$   
 $B(Z \rightarrow \mu e) < 10^{-17}$

# SUSY-GUT

LFV induced from finite slepton mixing through radiative correction

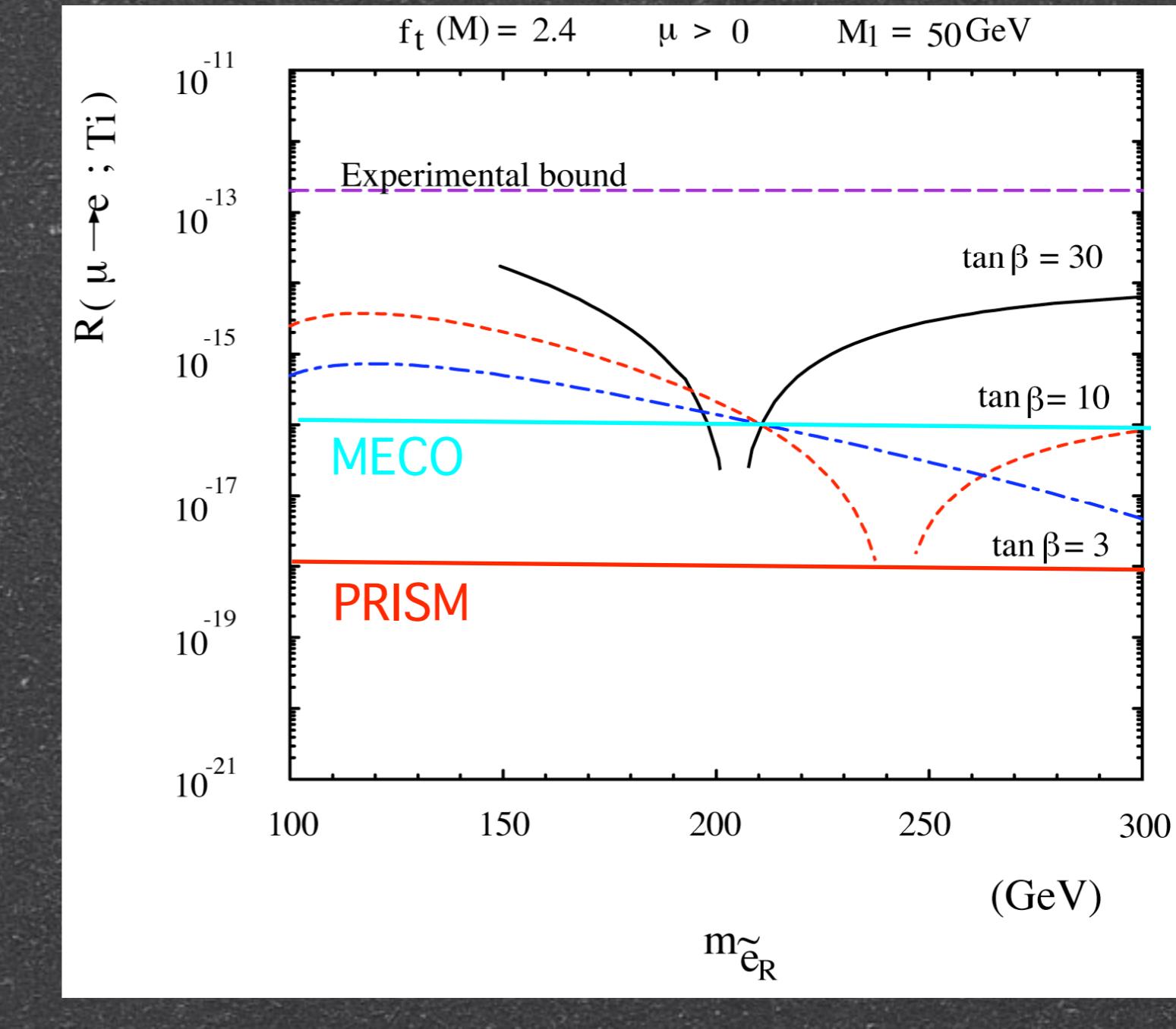


- SUSY SU(5) predictions

$$\text{BR}(\mu \rightarrow e\gamma) \approx 10^{-14} \div 10^{-13}$$

- SUSY SO(10) predictions

$$\text{BR}_{SO(10)} \approx 100 \text{ BR}_{SU(5)}$$

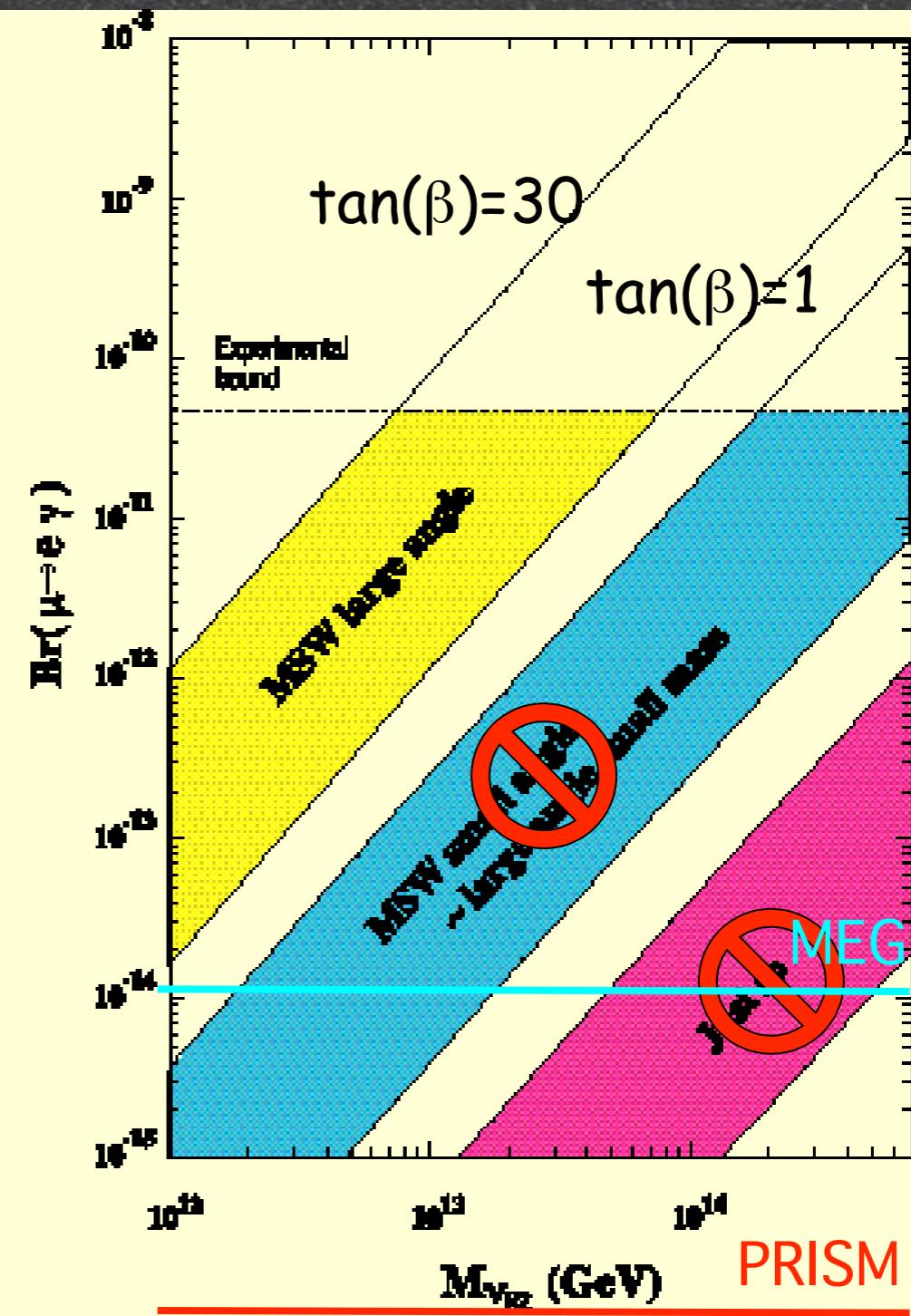
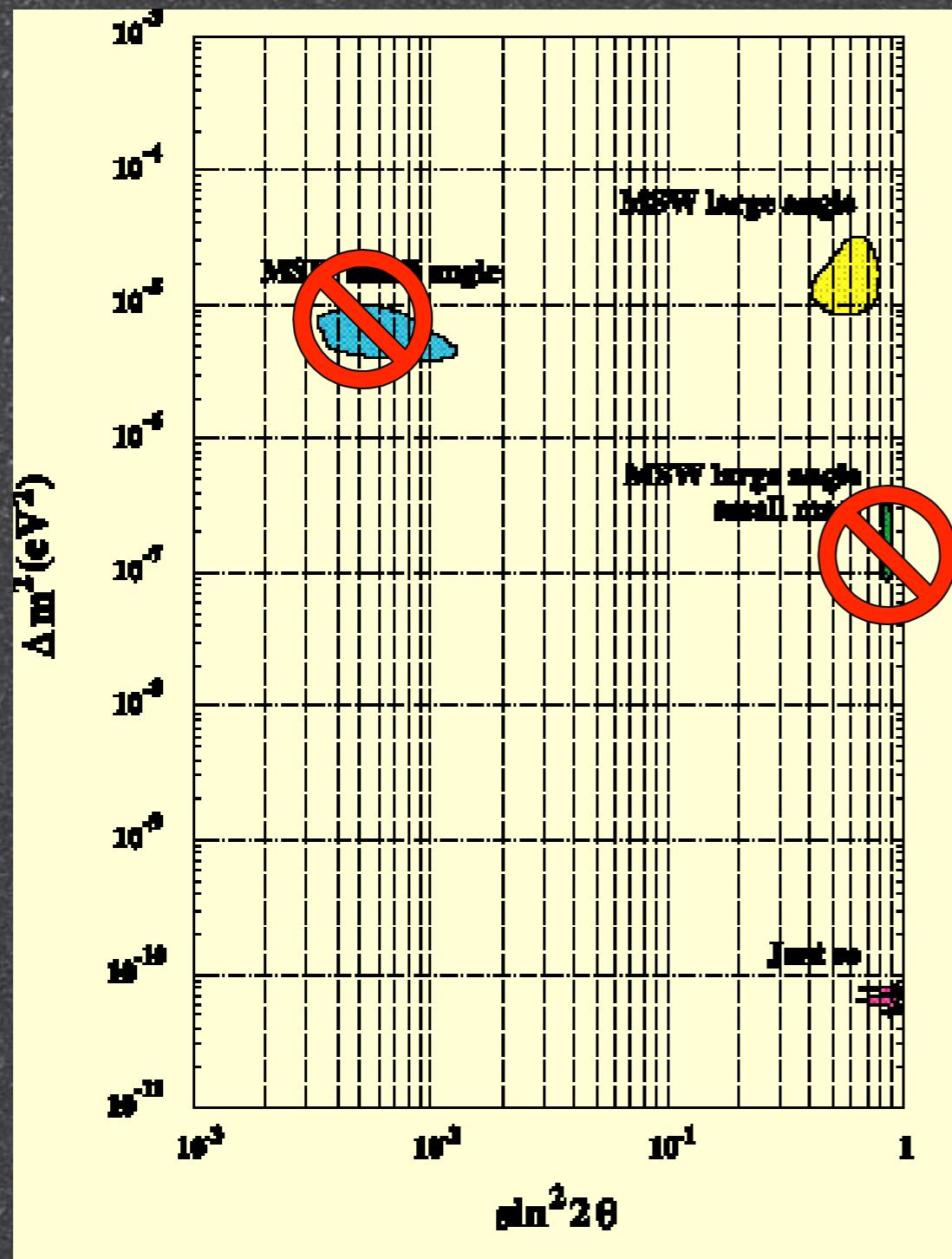


R. Barbieri et al., Phys. Lett. B338(1994) 212

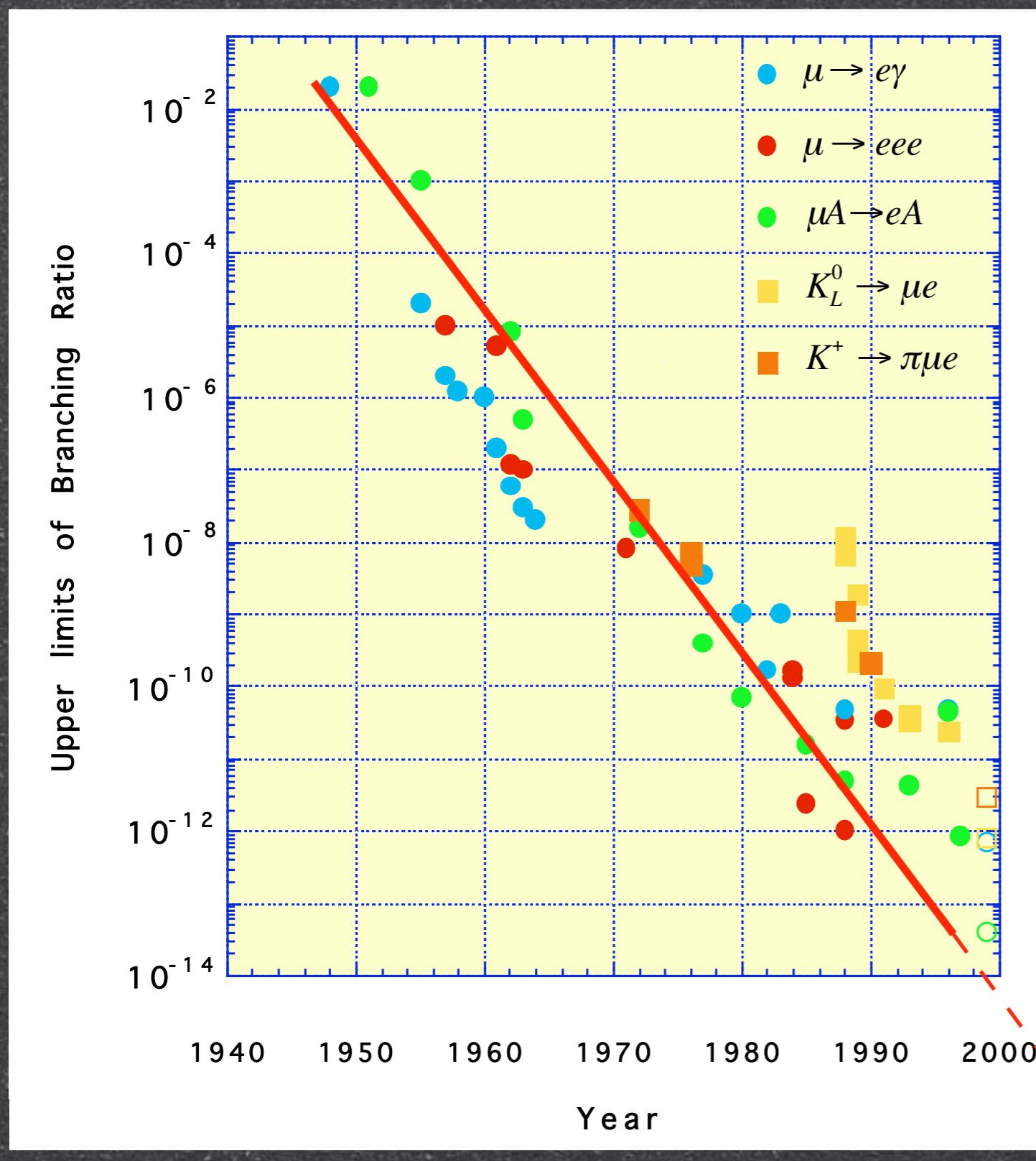
R. Barbieri et al., Nucl. Phys. B445(1995) 215

# MSSM with Seesaw Models

Neutrino Mixing  $\rightarrow$  Slepton Mixing  $\rightarrow$  Charged Lepton Mixing



# History of LFV Searches



Upper limits of Searches improved by two orders of magnitude per decade.

coming to  
 $10^{-16}$  to  $10^{-18}$

# Why Muon LFVs ?

Reaction	90 % CI	upper limit
$B(\mu^+ \rightarrow e\gamma)$	4.2	$\times 10^{-11}$
$B(\mu^+ \rightarrow e^+ e^- e^+)$	1.0	$\times 10^{-12}$
$B(\mu^- Ti \rightarrow e^- Ti)$	6.1	$\times 10^{-13}$
$B(\mu^- Pb \rightarrow e^- Pb)$	4.6	$\times 10^{-11}$
$B(\mu^- Ti \rightarrow e^+ Ca)$	1.7	$\times 10^{-12}$
$B(\mu^+ e^- \rightarrow \mu^- e^+)$	$G_{MM} < 3 \times 10^{-3} G_F$	
$B(\tau \rightarrow e\gamma)$	2.7	$\times 10^{-6}$
$B(\tau \rightarrow \mu\gamma)$	3.0	$\times 10^{-6}$
$B(\tau \rightarrow \mu\mu\mu)$	1.9	$\times 10^{-6}$
$B(\tau \rightarrow eee)$	3.3	$\times 10^{-6}$
$B(K_L \rightarrow \mu e)$	5.0	$\times 10^{-11}$
$B(\bar{K}^+ \rightarrow \pi^+ \mu^+ e^-)$	4.0	$\times 10^{-11}$
$B(K_L \rightarrow \pi^+ \mu^+ e^-)$	3.2	$\times 10^{-9}$
$B(D^0 \rightarrow \mu e)$	1.9	$\times 10^{-5}$
$B(D^0 \rightarrow \tau e)$	5.3	$\times 10^{-4}$
$B(D^0 \rightarrow \Phi \mu e)$	3.4	$\times 10^{-5}$
$B(B \rightarrow \mu e)$	5.9	$\times 10^{-6}$
$B(B \rightarrow K \mu e)$	1.8	$\times 10^{-5}$
$B(Z^0 \rightarrow \mu e)$	2.3	$\times 10^{-6}$
$B(Z^0 \rightarrow \tau e)$	7.3	$\times 10^{-6}$
$B(Z^0 \rightarrow \tau \mu)$	1.0	$\times 10^{-5}$

beam will increase  
by  $10^4$

beam will increase  
by  $10^2$

The muon might

be the best

# LFV Catalog

For the muons,

$\Delta L = 1$

- $\mu^+ \rightarrow e^+ \gamma$
- $\mu^+ \rightarrow e^+ e^+ e^-$
- $\mu^- + N(A, Z) \rightarrow e^- + N(A, Z)$

- 
- $\mu^- + N(A, Z) \rightarrow e^+ + N(A, Z - 2)$

$\Delta L = 2$

- $\mu^+ e^- \rightarrow \mu^- e^+$
- $\mu^- + N(A, Z) \rightarrow \mu^+ + N(A, Z - 2)$
- $\nu_\mu + N(A, Z) \rightarrow \mu^+ + N(A, Z - 1)$
- $\nu_\mu + N(A, Z) \rightarrow \mu^+ \mu^+ \mu^- + N(A, Z - 1)$

# What is $\mu \rightarrow e\gamma$ ?

## ■ Event Signature

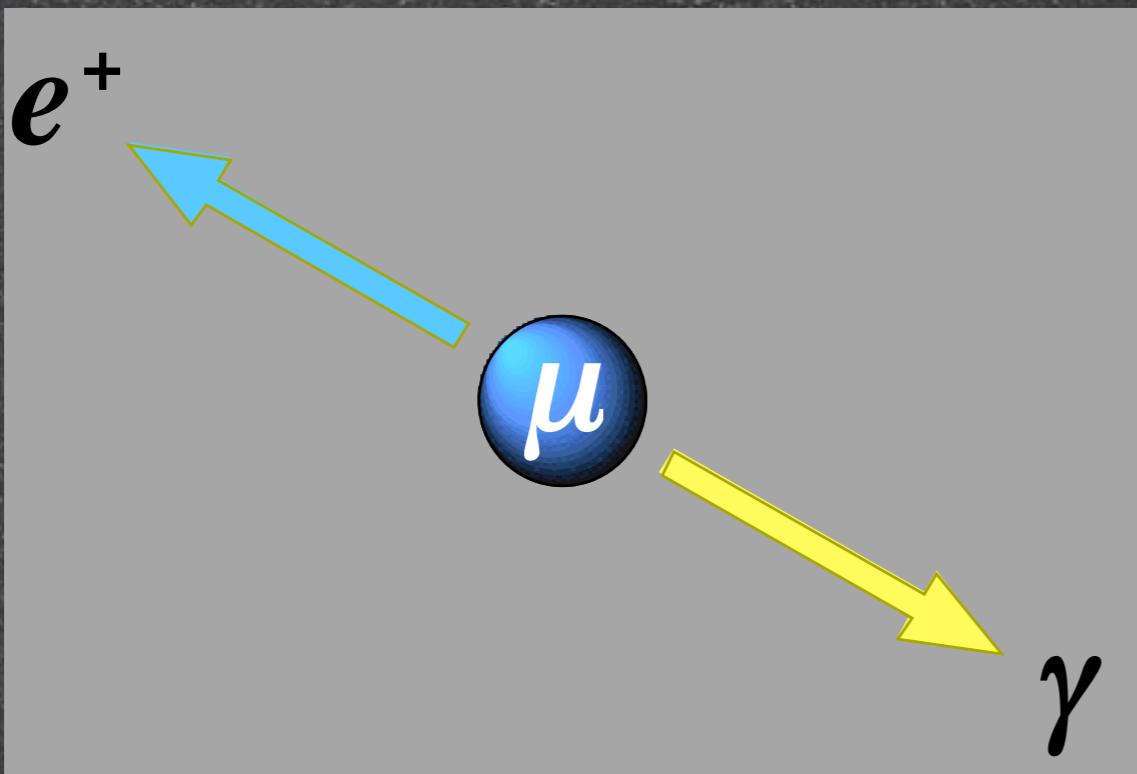
- $E_e = m_\mu/2, E_\gamma = m_\mu/2$  ( $= 52.8$  MeV)
- angle  $\theta_{e\gamma} = 180$  degrees (back-to-back)
- time coincidence

## ■ Backgrounds

- prompt physics background
  - radiative muon decay  $\mu \rightarrow e\nu\nu\gamma$ 
    - when two neutrinos carry very small energies.....

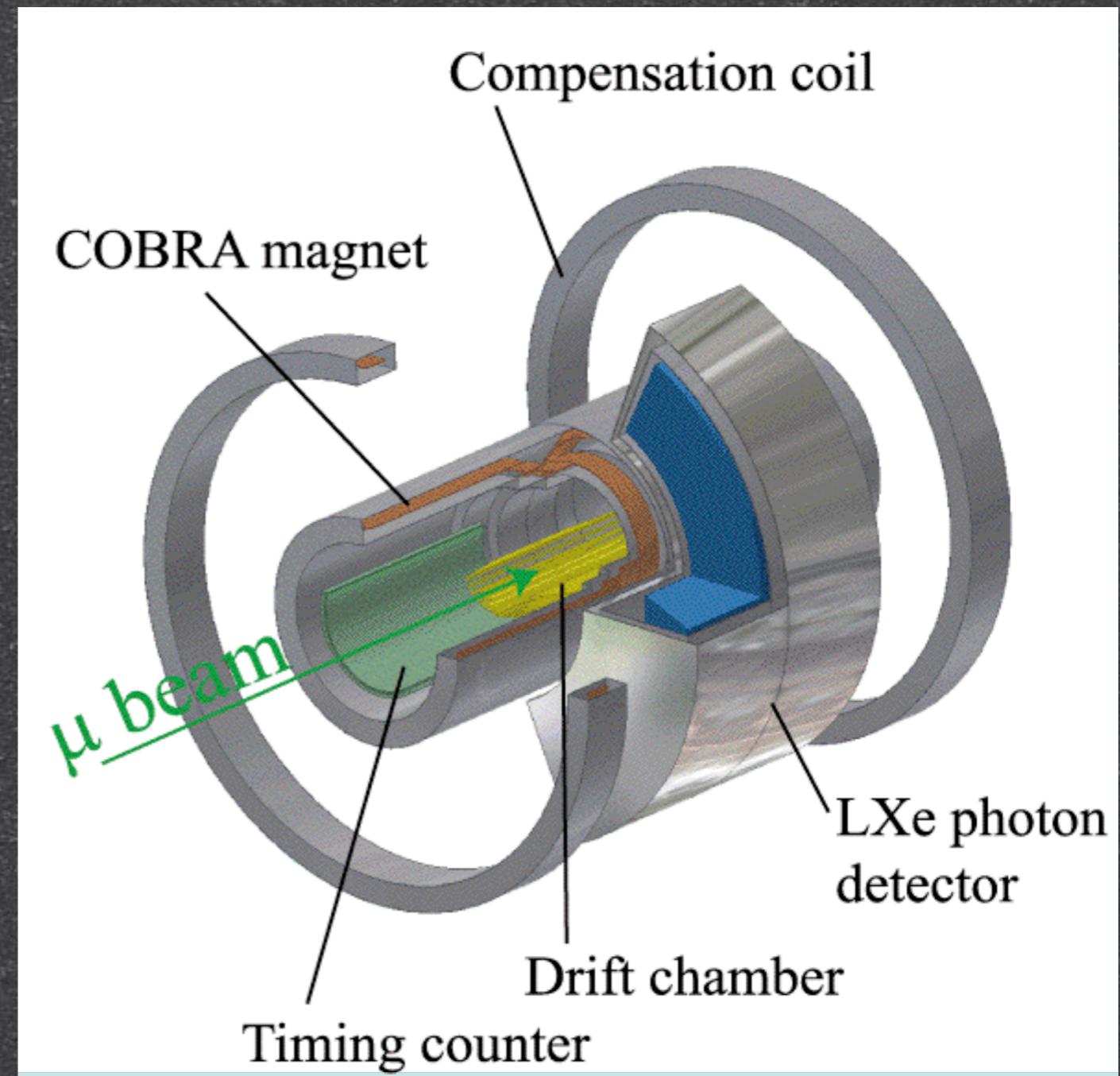
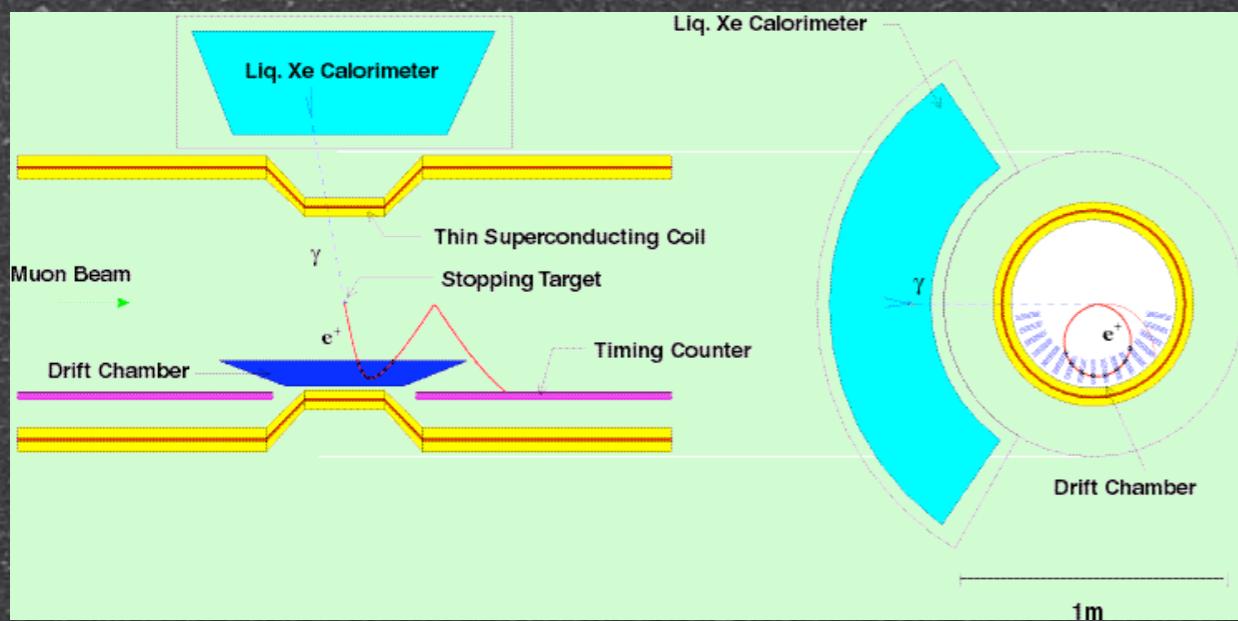
## ■ accidental background

- positron  $e^+$  in  $\mu \rightarrow e\nu\nu$
- photon  $\gamma$  in  $\mu \rightarrow e\nu\nu\gamma$  in  $e^+e^-$  annihilation in flight



# MEG at PSI

- $\mu \rightarrow e \gamma$ 
  - MEG at PSI, 2004~
    - DC beam  $10^8 \mu/\text{s}$
    - BR  $\sim 10^{-13}$
  - Accidental background
  - Detector Improvement
  - Polarization



# Accidental Background

$$\text{Accidental Background} \propto (R_\mu)^2 \times \Delta E_e \times (\Delta E_\gamma)^2 \times \Delta t_{e\gamma} \times (\Delta \theta_{e\gamma})^2$$

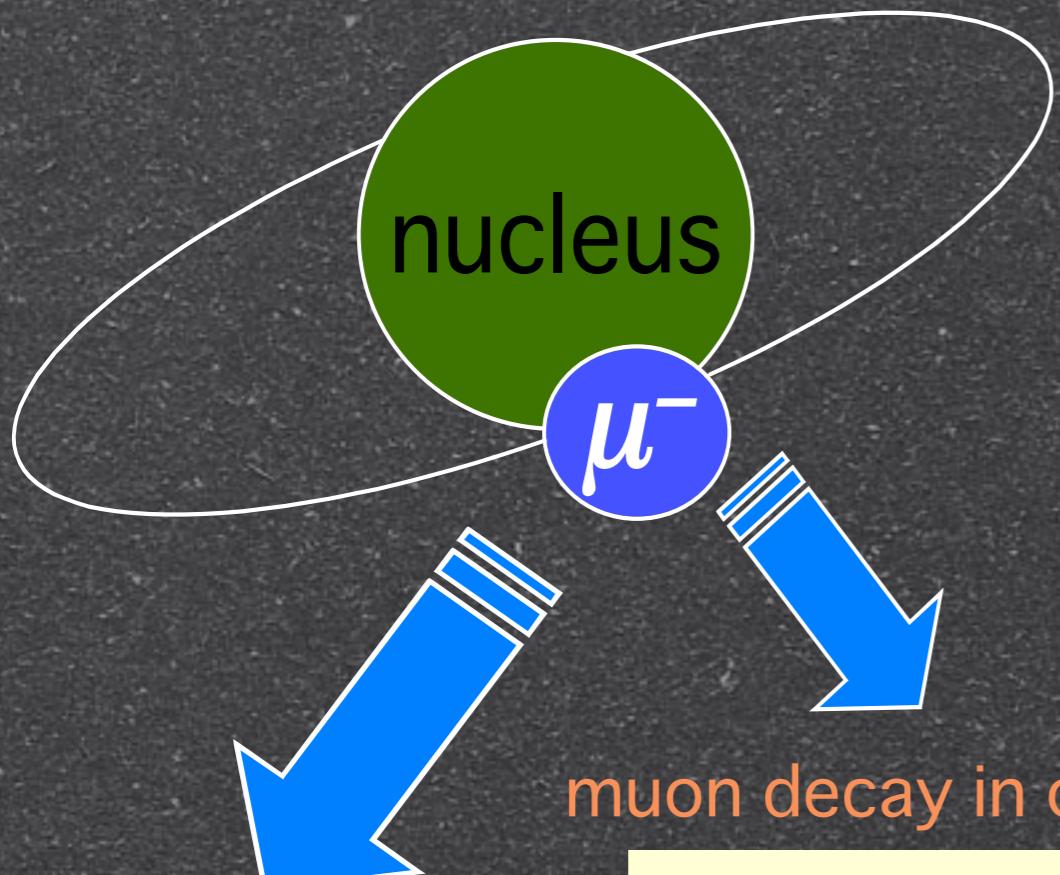
Place	Year	$\Delta E_e$	$\Delta E_\gamma$	$\Delta t_{e\gamma}$	$\Delta \theta_{e\gamma}$	$R_\mu$	Upper Limit	References
SIN	1977	8.7%	9.3%	1.4 ns	-	$5 \times 10^5$	$< 1.0 \times 10^{-9}$	A. Van der Schaaf, <i>et al.</i> , NP A340(1980)249
TRIUMF	1977	10%	8.7%	6.7 ns	-	$2 \times 10^5$	$< 3.6 \times 10^{-9}$	P. Depommier <i>et al.</i> , PRL 39(1977)1113
LANL	1979	8.8%	8%	1.9 ns	37 mrad	$2.4 \times 10^6$	$< 1.7 \times 10^{-10}$	W.W. Kinnison <i>et al.</i> , PR D25(1982)2846
Crystal Box	1986	8%	8%	1.8 ns	87 mrad	$4 \times 10^5$	$< 4.9 \times 10^{-11}$	R.D. Bolton, <i>et al.</i> , PR D38(1988)2077
MEGA	1999	1.2%	4.5%	1.6 ns	17 mrad	$2.5 \times 10^8$	$< 1.2 \times 10^{-11}$	M.L. Brooks, <i>et al.</i> , PRL 83(1999)1521
PSI	2004?	0.7%	1.4%	0.15 ns	12 mrad	$10^8$	$< 10^{-14}$	T. Mori, <i>et al.</i> , Research Proposal to PSI (1999)

$B_{\mu \rightarrow e\gamma} = 10^{-14}$   
 $N_b = 0.5 \text{ events}$

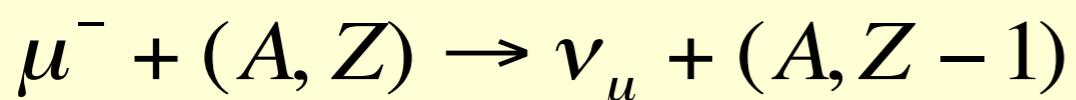
$B_{\mu \rightarrow e\gamma} = 10^{-16}$   
•  $R_\mu = 10^{10} \mu/\text{s}$   
•  $N_b \sim 10^4 \text{ events?}$

# What is $\mu$ -e conversion?

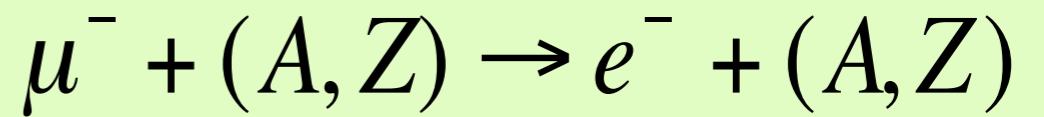
1s state in a muonic atom



nuclear muon capture



Neutrino-less muon nuclear capture  
(= $\mu$ -e conversion)

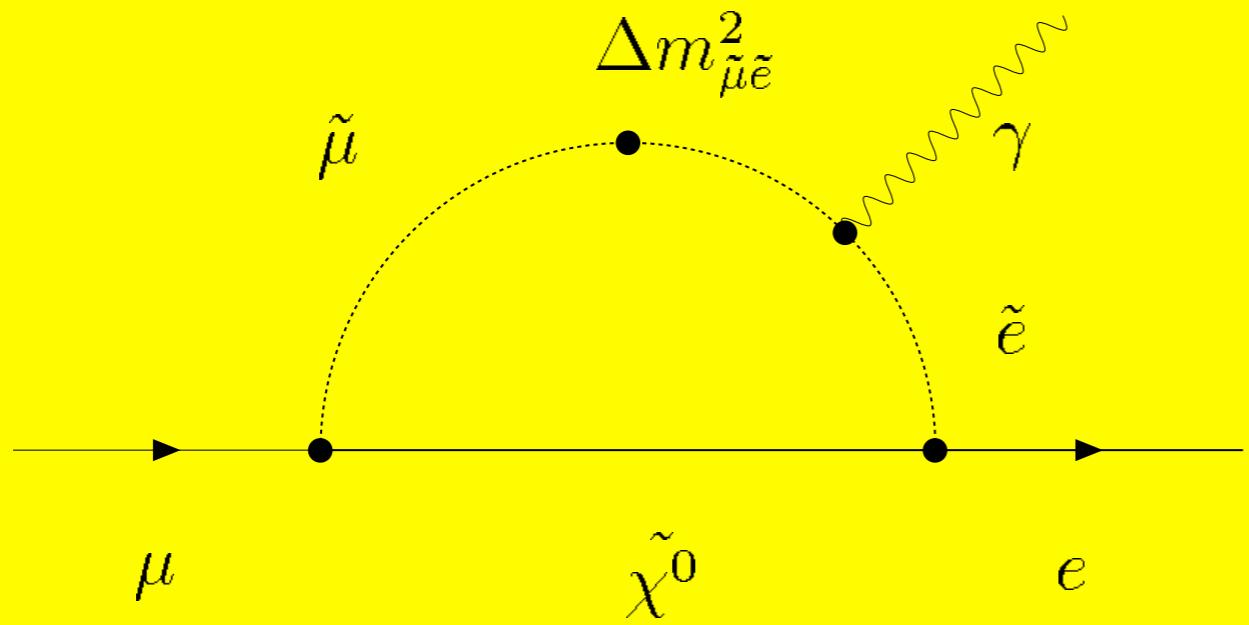


lepton flavors changes by one unit.

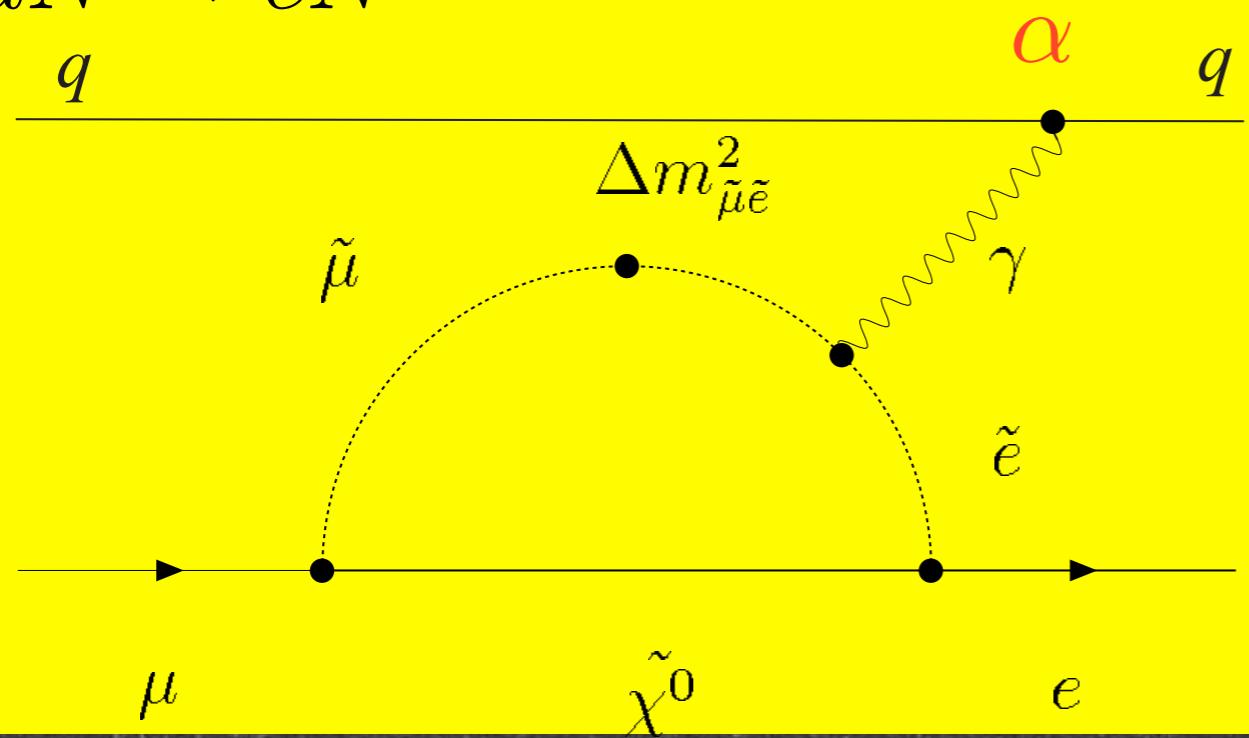
$$B(\mu^- N \rightarrow e^- N) = \frac{\Gamma(\mu^- N \rightarrow e^- N)}{\Gamma(\mu^- N \rightarrow \nu N)}$$

# Photon-mediated LFV

$\mu \rightarrow e\gamma$



$\mu N \rightarrow e N$



$\mu - e$  conversion vs.  
 $\mu \rightarrow e\gamma$

If photon-mediated,

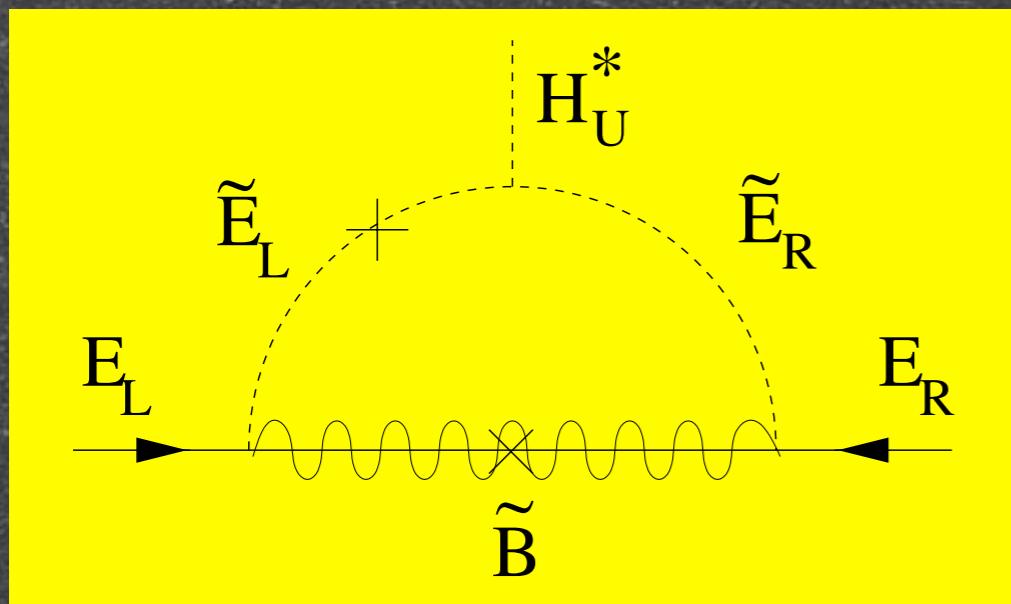
$$\frac{B(\mu N \rightarrow e N)}{B(\mu \rightarrow e\gamma)} \sim \frac{1}{100}$$

But, experimentally,

$\mu \rightarrow e\gamma$	$< 1.2 \times 10^{-11}$
$\mu N \rightarrow e N$	$< 6 \times 10^{-13}$

# Higgs-mediated SUSY LFV

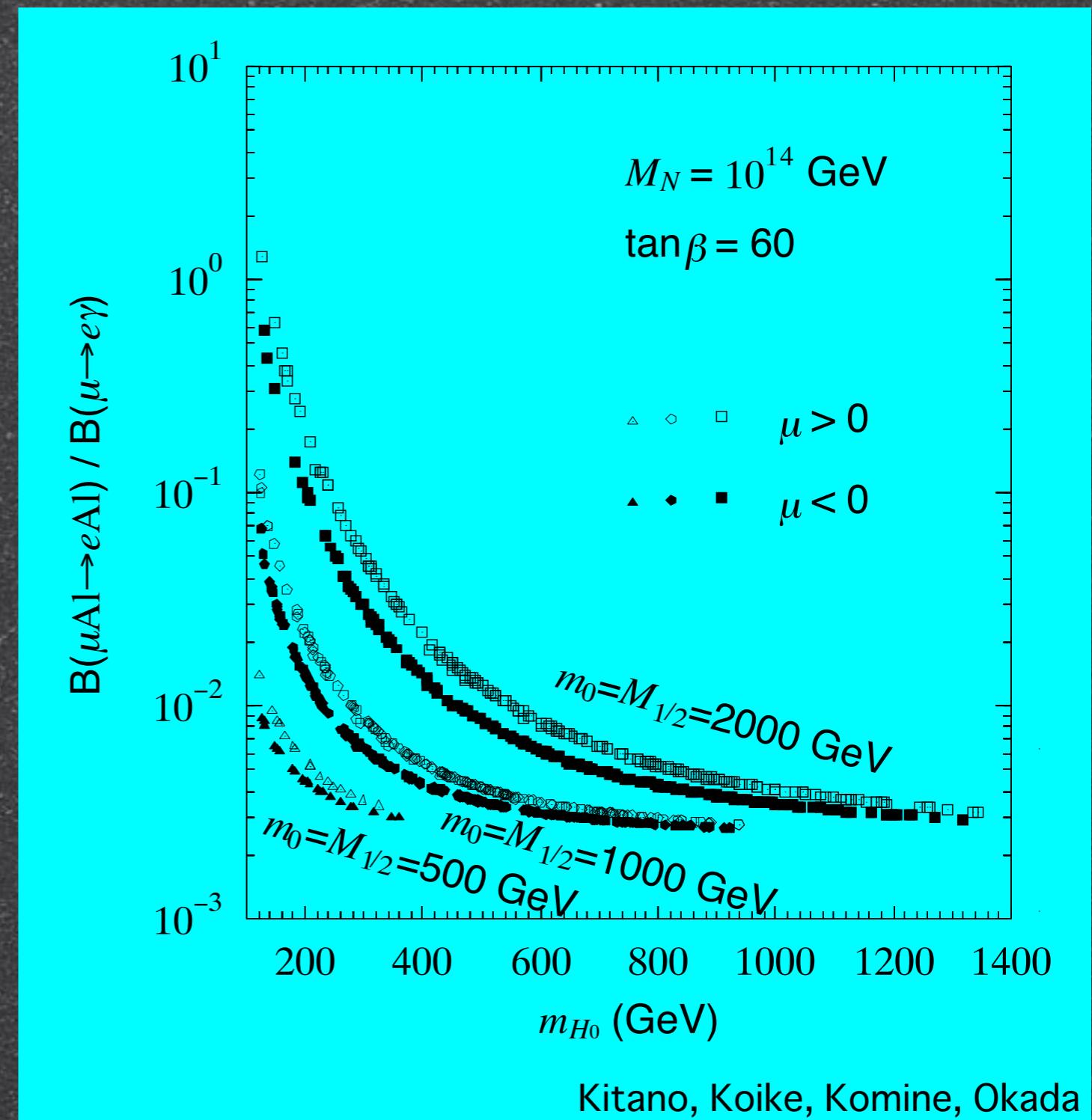
Higgs-exchange for LFV in SUSY Seesaw model



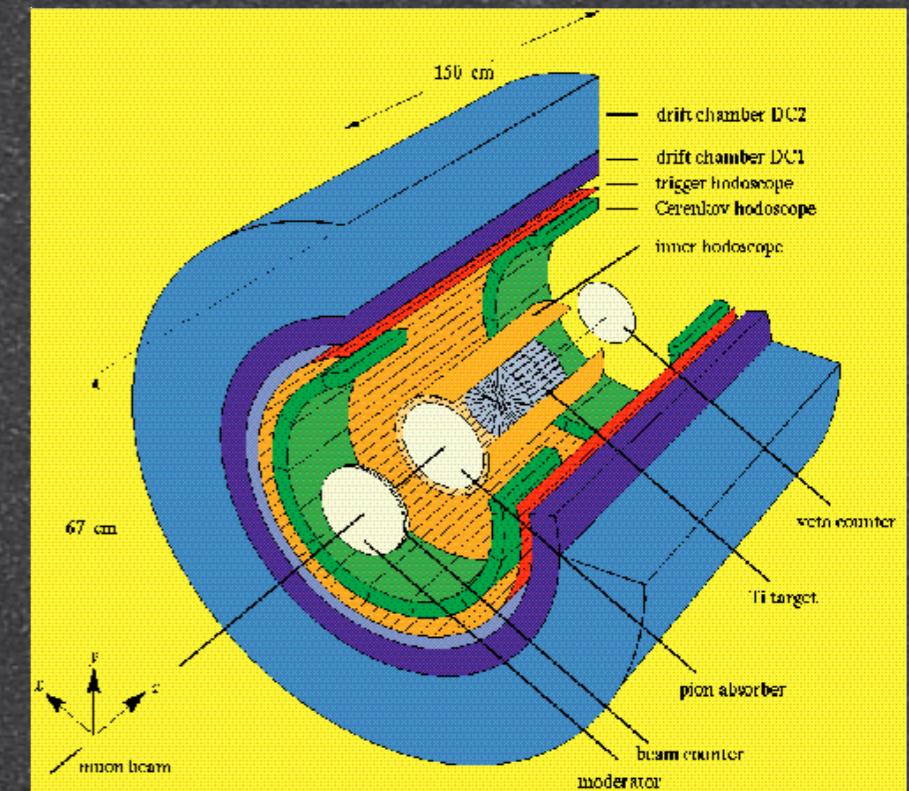
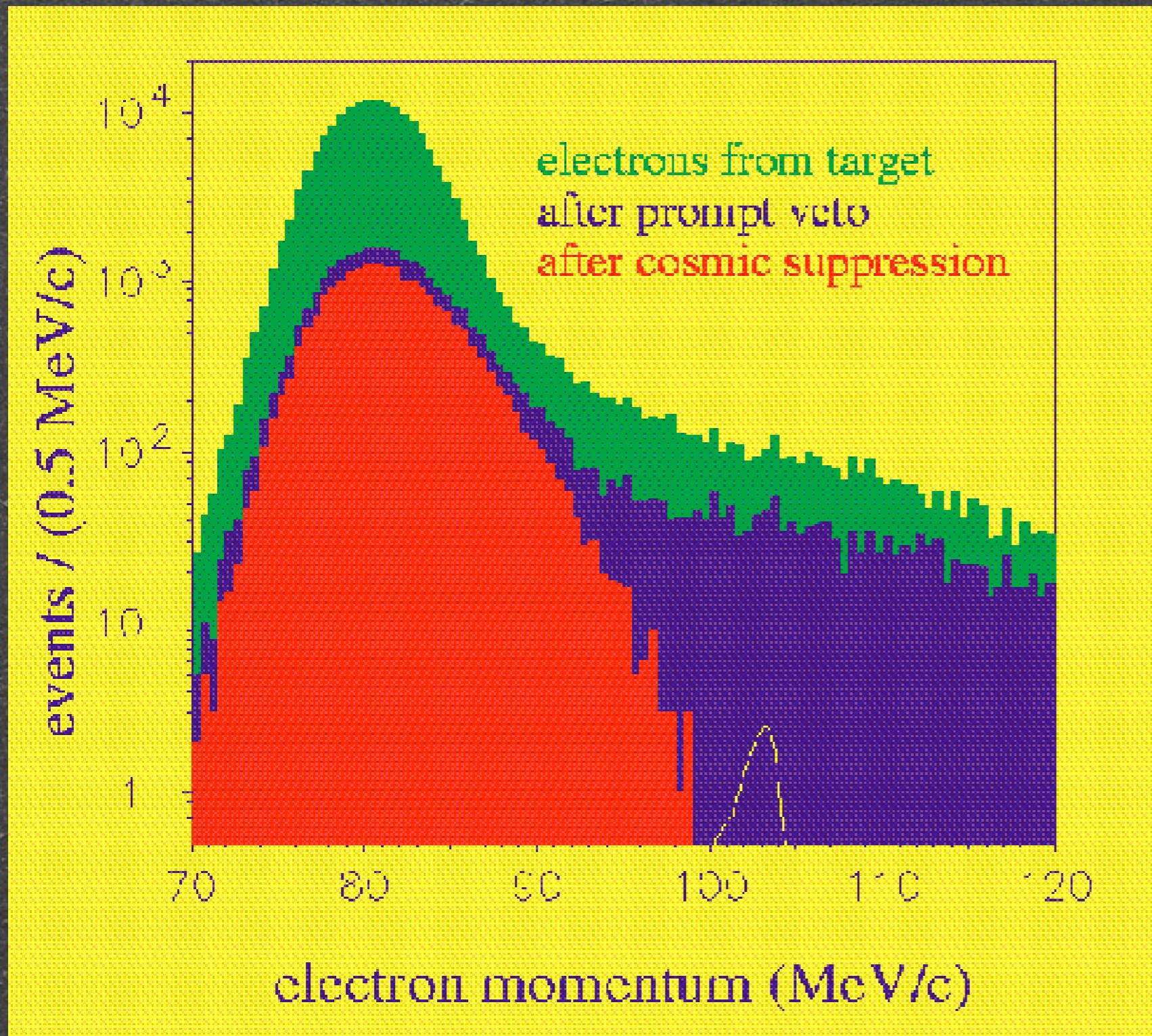
When  $H_0$  mass is small,  
Higgs-mediated diagram  
contributes more.

$$\frac{B(\mu N \rightarrow e N)}{B(\mu \rightarrow e\gamma)} \sim O(1)$$

at  $H_0 \sim 200$  GeV



# SINDRUM-II Results

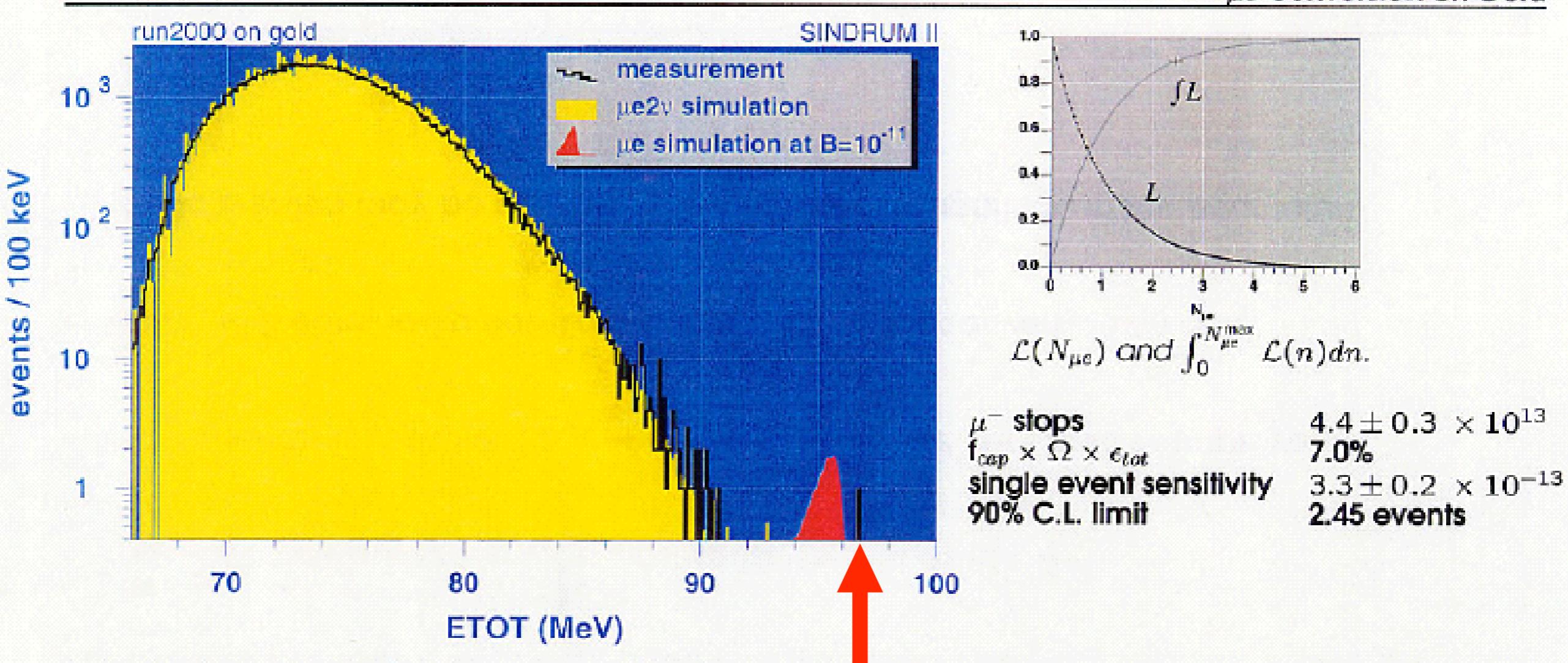


Sindrum-II  
1993 result

$$B(\mu^- + Ti \rightarrow e^- + Ti) < 6.1 \times 10^{-13}$$

# SINDRUM-II Results

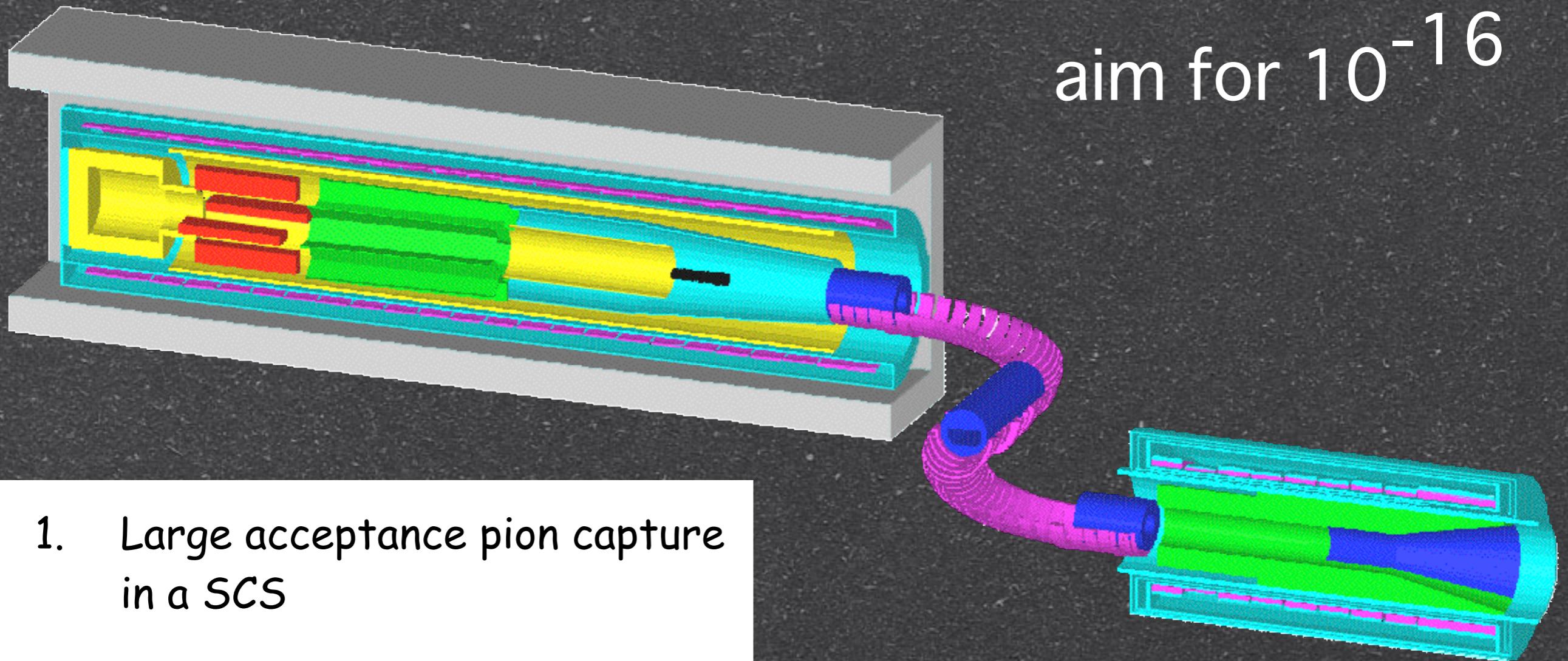
## Final result



In the likelihood analysis of the energy distribution a flat background from cosmic rays and radiative pion capture was allowed.

Result:  $B_{\mu e}^{\text{gold}} < 8 \times 10^{-13}$  90% C.L.

# MECO at BNL



1. Large acceptance pion capture in a SCS
2. Muon transport ( $60 - 120$   $\text{MeV}/c$ ) in a curved solenoid
3. Long detector solenoid with muon stopping target and tracking system

aim for  $10^{-16}$

R&D money in US-FY2004.  
Construction money  
in US-FY2006.

# Which Muon LFV Process Next ?

	issue	beam requirement
$\mu \rightarrow e\gamma$	detector-limited	a continuos beam
$\mu \rightarrow eee$	detector-limited	a continuos beam
$\mu N \rightarrow eN$	beam-limited	a pulsed beam